

Changes in GEBV in ssGBLUP with inversion by the APY algorithm using different core animals

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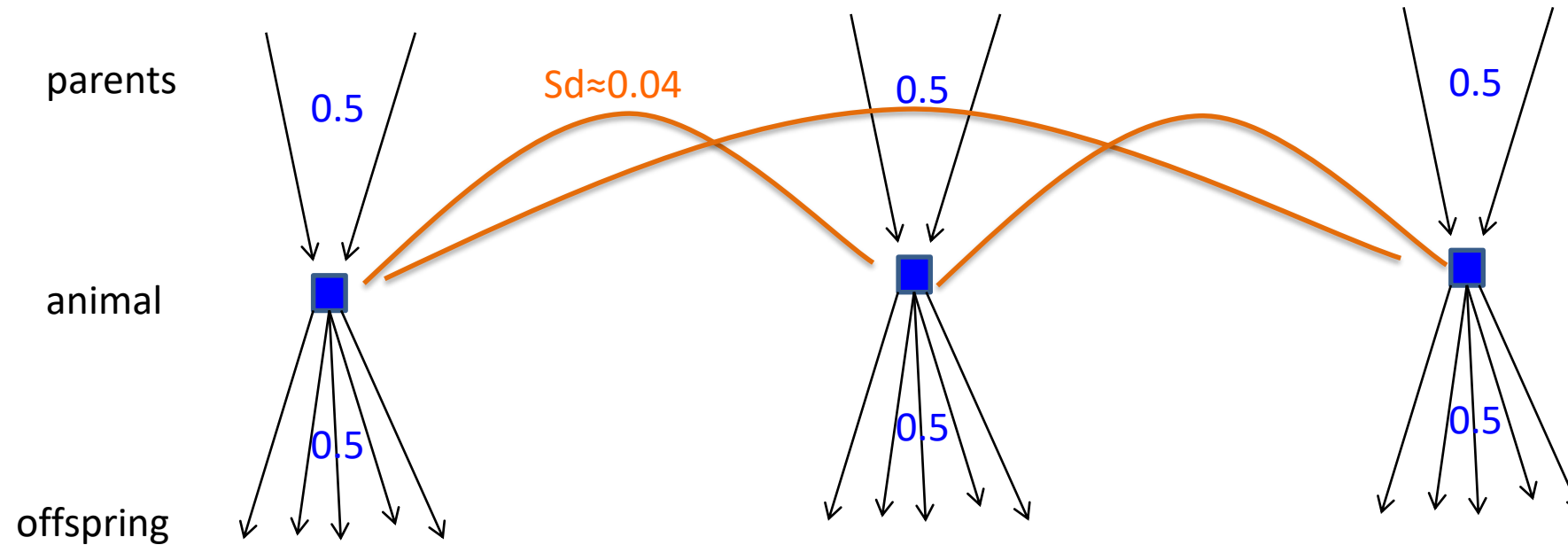
APY algorithm and different sets of core animals

- ssGBLUP used routinely in chicken, pigs and beef
- Inverse of G by APY to reduce costs
 - Up to 2.3 million genotyped animals
- Reports of GEBV changes with different core animals
- Why and how much?

Changes in nongenomic and genomic evaluations

- Little change in BLUP for older animals
 - Fixed effects stable
 - New relationships little affect older animals
- More change in genomic evaluation
 - Each new genotyped animal affects other genotyped animals
 - Details matter

BLUP and genomics



BLUP

$$u_i = (u_{\text{sire}} + u_{\text{dam}}) / 2 + \varphi$$

Genomics

$$u_i = \mathbf{P}u_{i-1} + \varepsilon$$

Genomic evaluations less stable than BLUP

Origin of changes with APY

Genomic relationship matrix – information + noise

$$\mathbf{u}_n = \mathbf{P}\mathbf{u}_c + \boldsymbol{\varepsilon}$$

$$\text{var}(\boldsymbol{\varepsilon}_i) = \mathbf{g}_{ii} - \mathbf{g}_{i,c}\mathbf{G}^{cc}\mathbf{g}_{c,i}$$

$$\sigma_a^2 \quad \eta\sigma_a^2 \quad (1 - \eta)\sigma_a^2$$

0.98

0.02

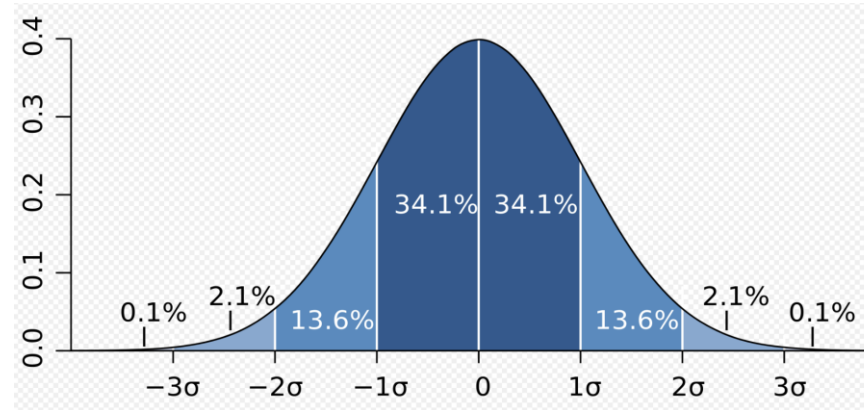
$$\text{sd}(\boldsymbol{\varepsilon}) = \sigma_a \sqrt{(1 - \eta)} \quad \text{Main source of noise}$$

Approx. difference between GEBV with 2 random cores:

$$\text{sd}(\boldsymbol{\varepsilon}_1 - \boldsymbol{\varepsilon}_2) \approx 1.4 \sigma_a \sqrt{(1 - \eta)} \text{ rel}$$

Outliers in normal distribution

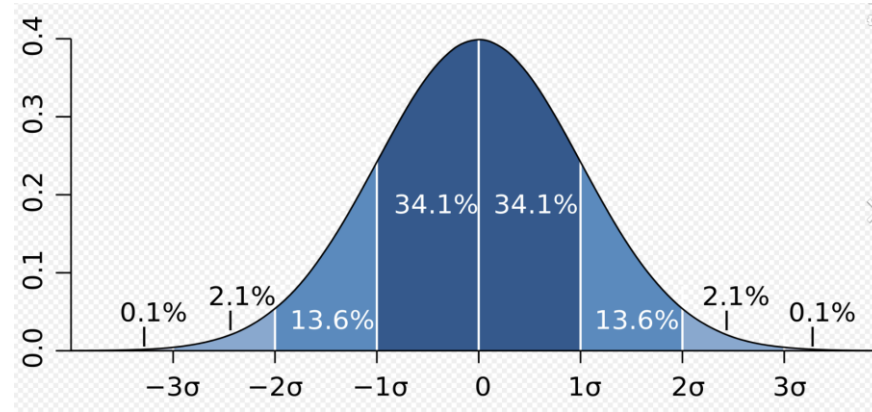
$$\varepsilon_1 - \varepsilon_2 \sim 1.4 \text{ rel } N(0, 0.02) \sigma_a^2$$



| Samples | Avg N(0, 1) |
|------------------|---------------|
| All | 0.8 |
| Top 1 in 100 | 2.9 |
| Top 1 in 10,000 | 4.1 |
| Top 1 in million | 5.0 |

Outliers in normal distribution

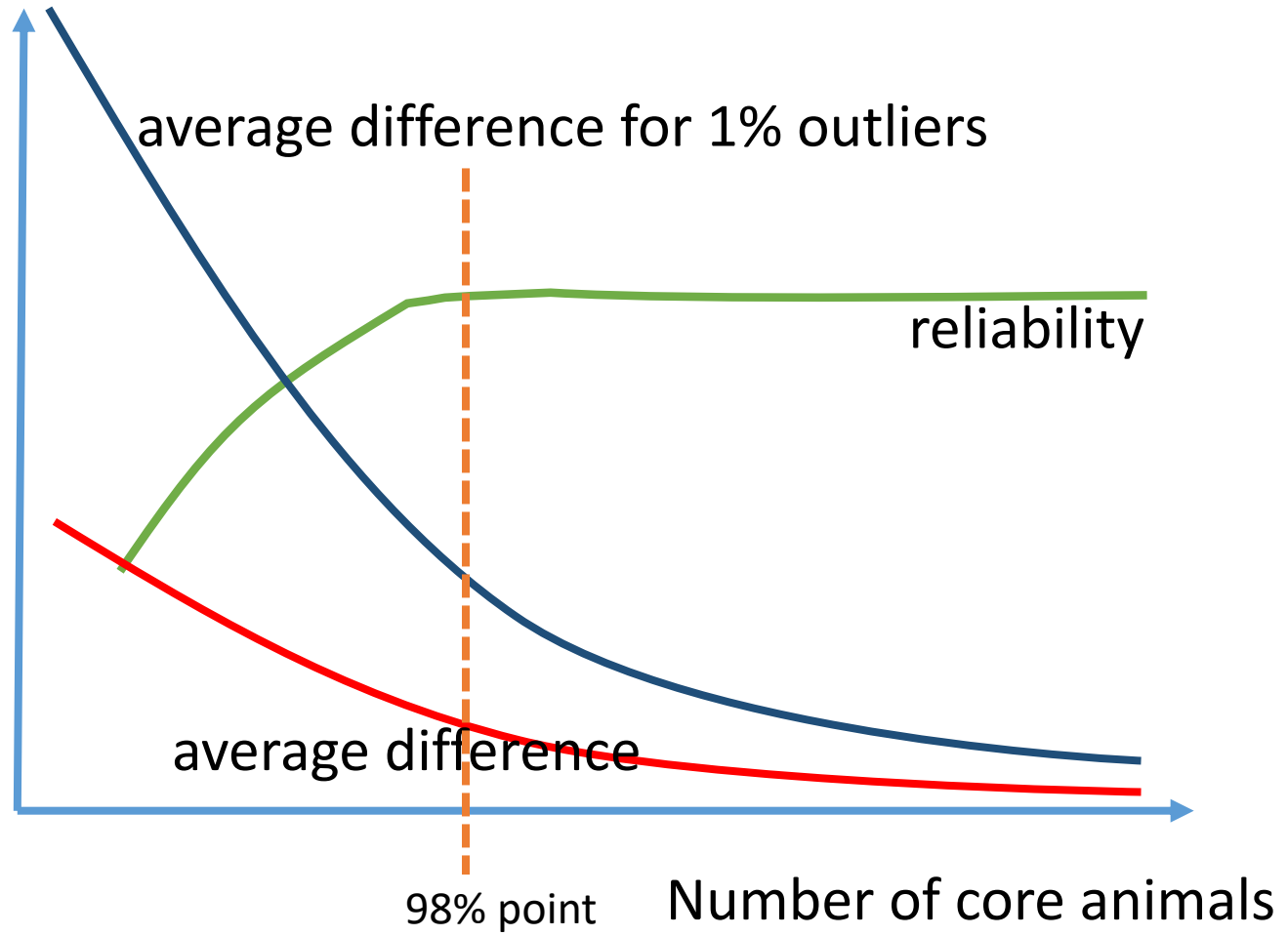
$$\varepsilon_1 - \varepsilon_2 \sim 1.4 \text{ rel } N(0, 0.02) \sigma_a^2$$



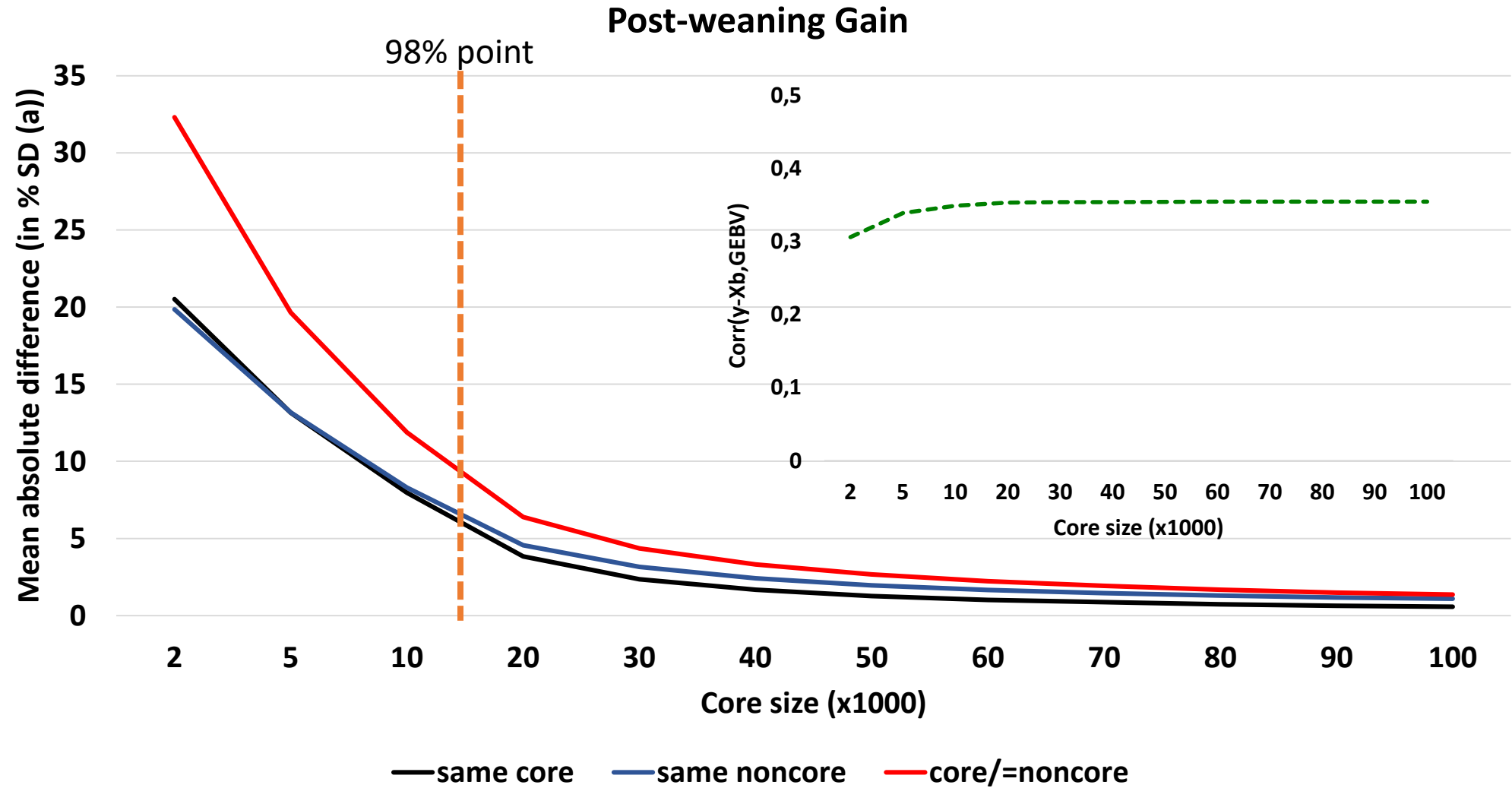
| Samples | Avg N(0, 1) | Avg($\varepsilon_1 - \varepsilon_2$ |
|------------------|---------------|--|
| All | 0.8 | 0.09 |
| Top 1 in 100 | 2.9 | 0.35 |
| Top 1 in 10,000 | 4.1 | 0.49 |
| Top 1 in million | 5.0 | 0.60 |

Rel=0.6

Theoretical reliability and average differences

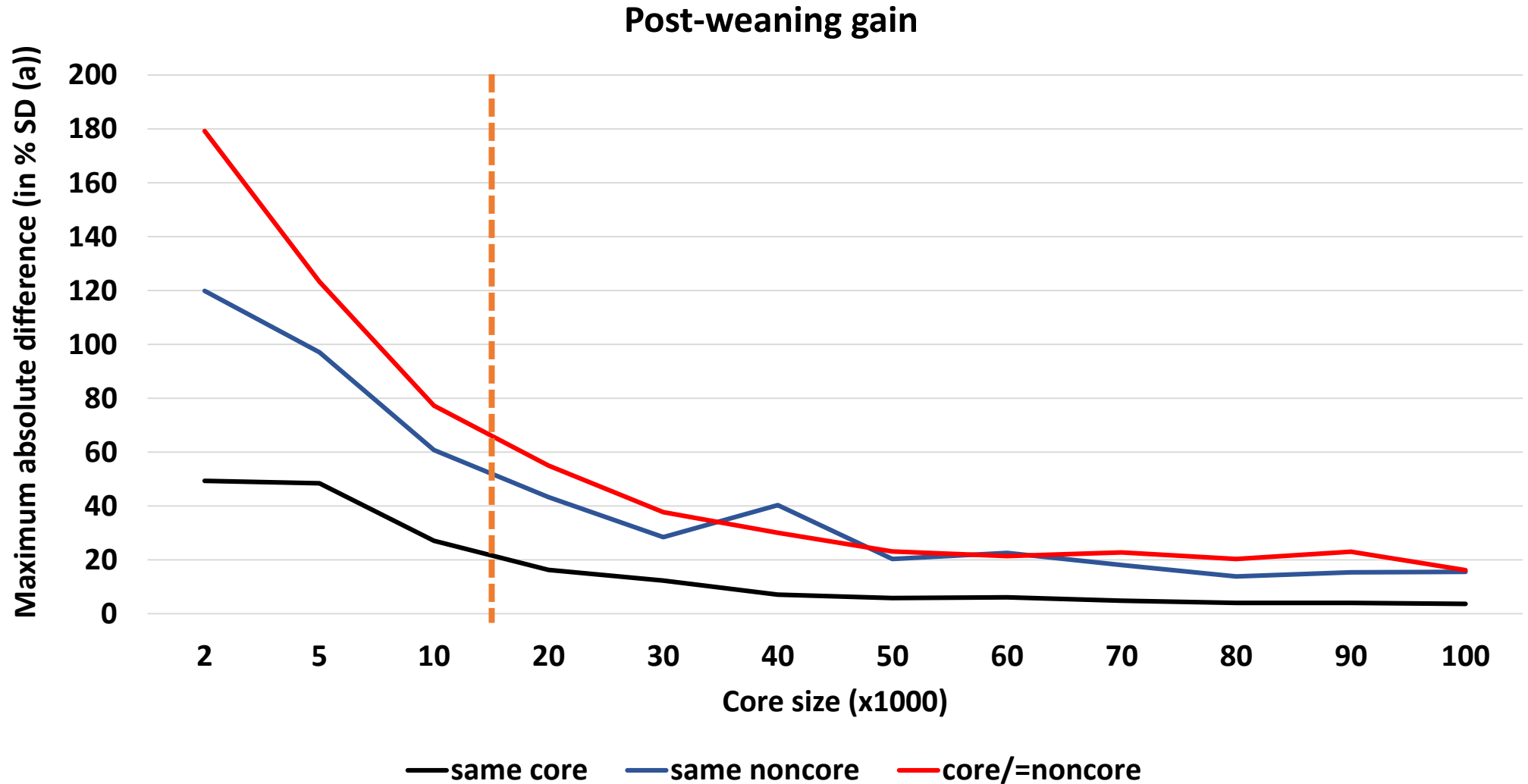


Mean change for Angus



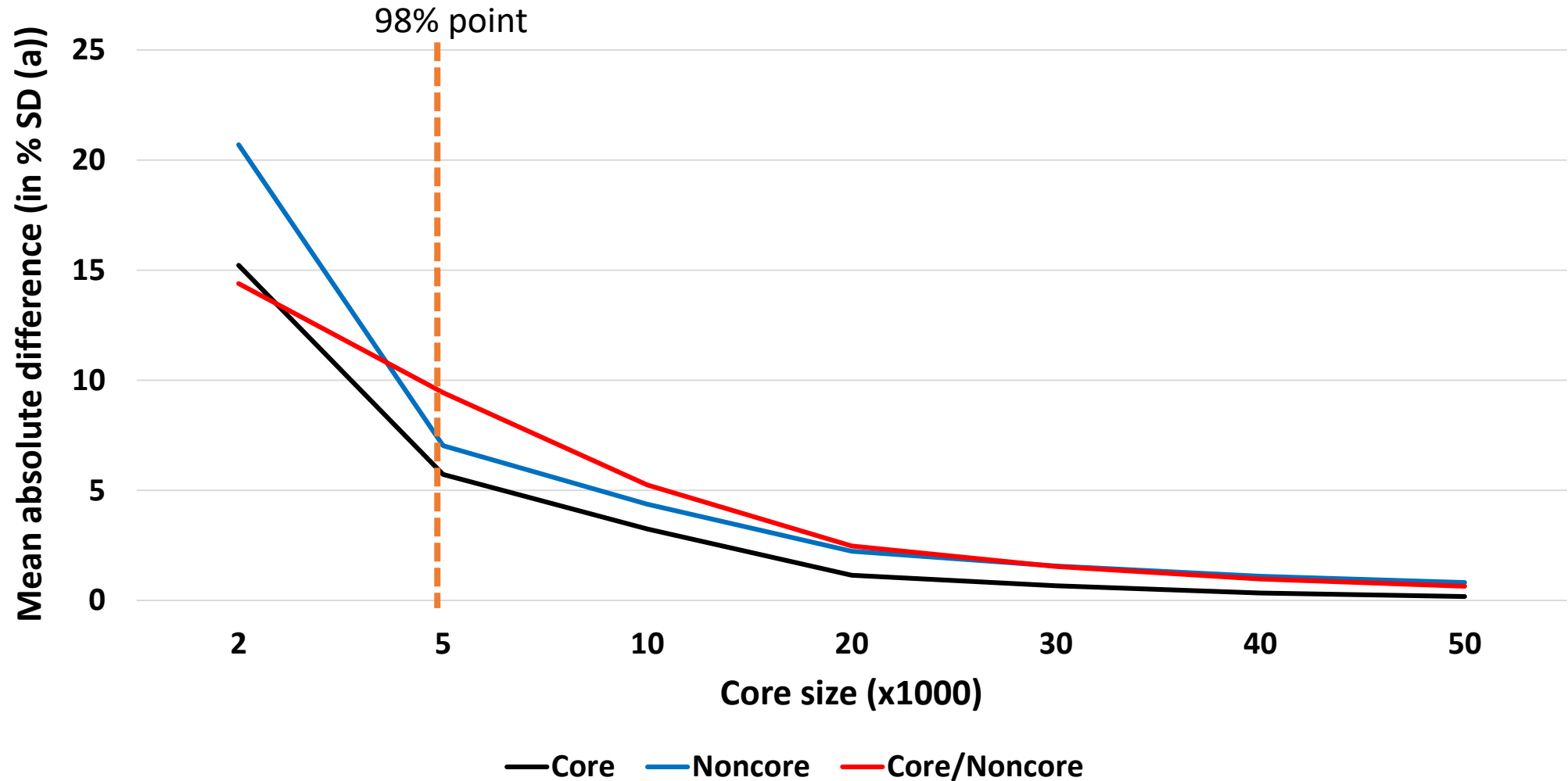
Maximum change for Angus

SD (a) = 27

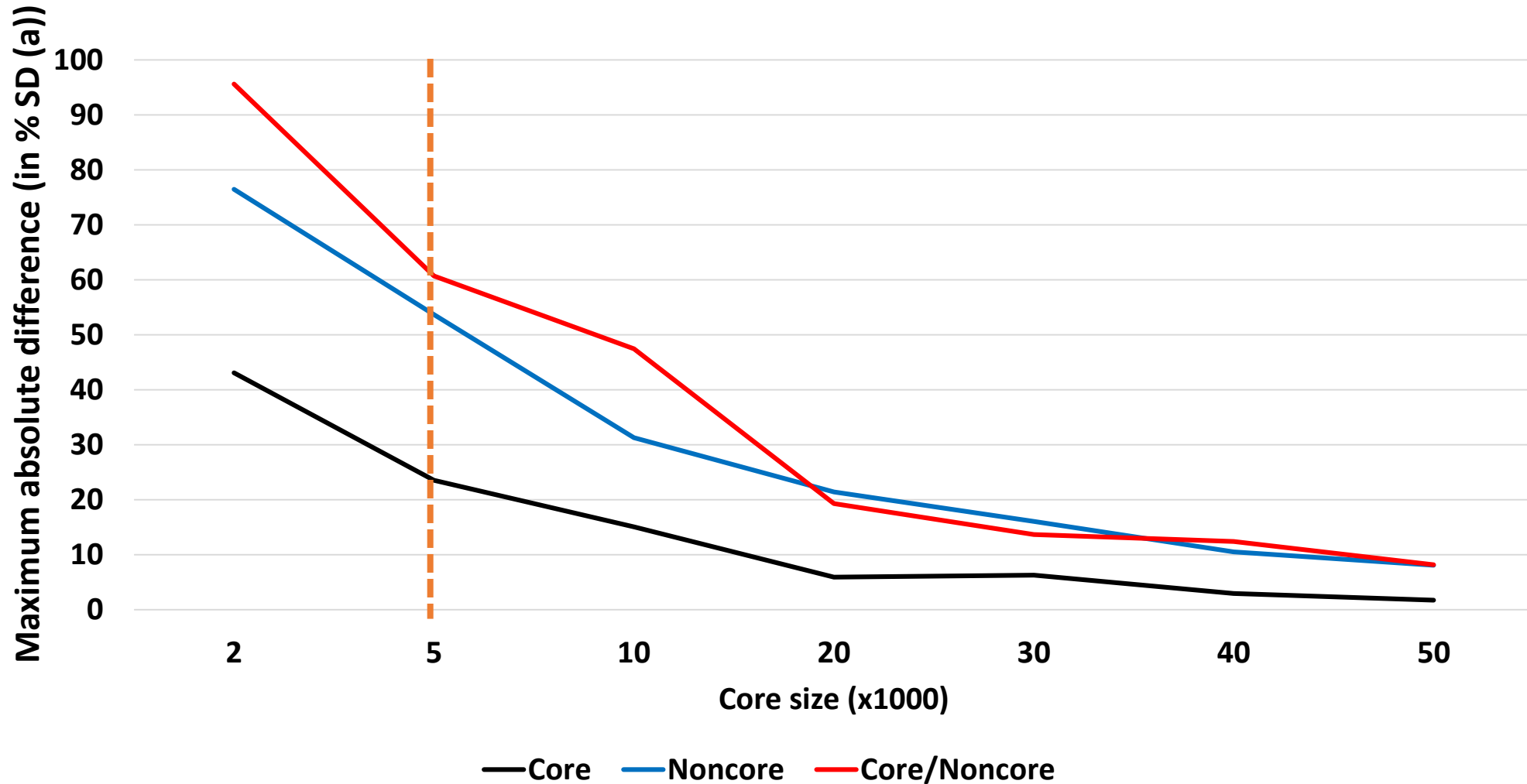


Mean change for Pigs

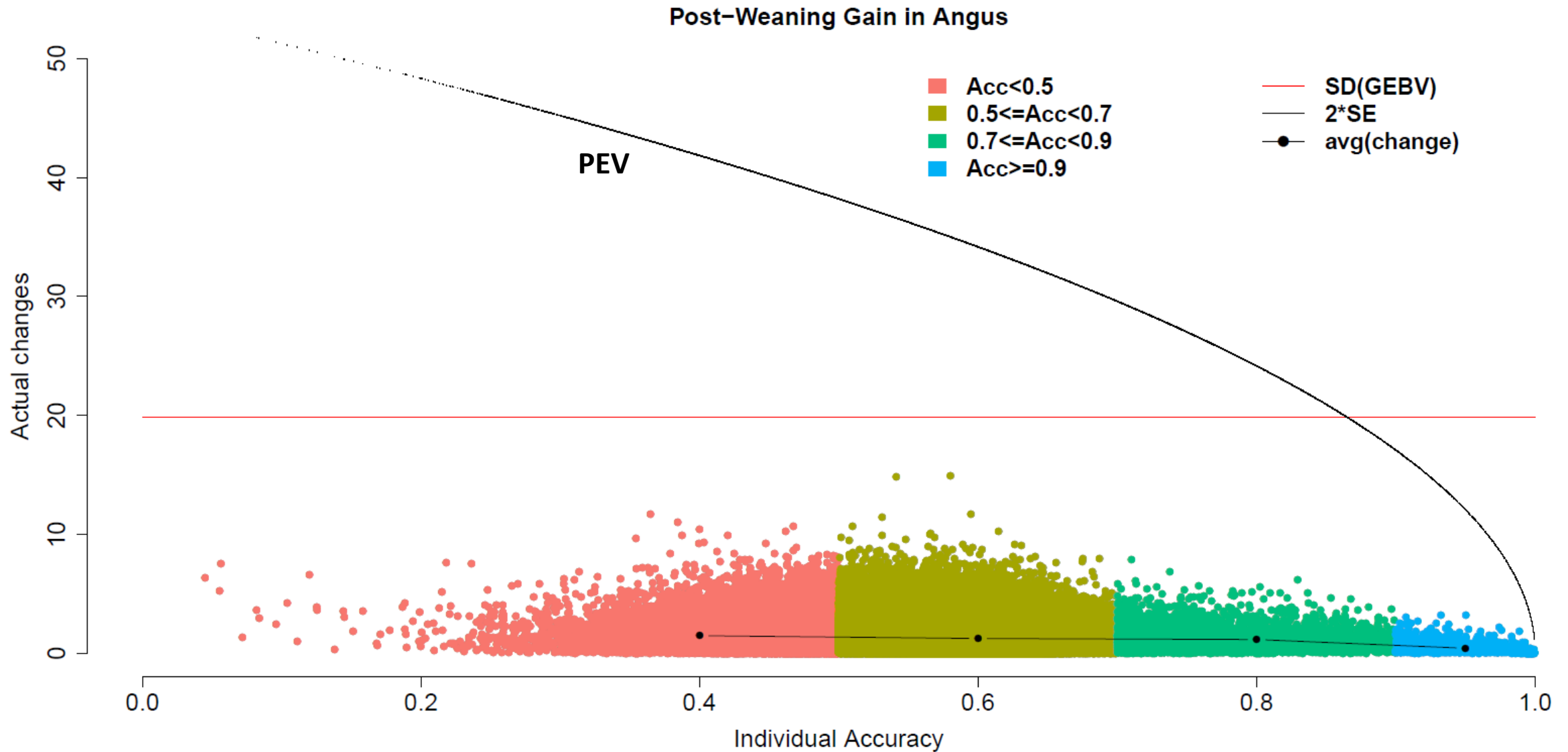
SD (a) = 39



Maximum change for Pigs



Which animals change most?



How to minimize changes due to APY?

- Increase number of core animals
- Treat important animals as core
- Keep core animals same for some period (e.g., 1 year)
- Use indirect prediction
- Use groups of bulls

Average change for outliers

$$GEBV = rel * BV + rel(1 - rel)N(0, \sigma_a^2)$$

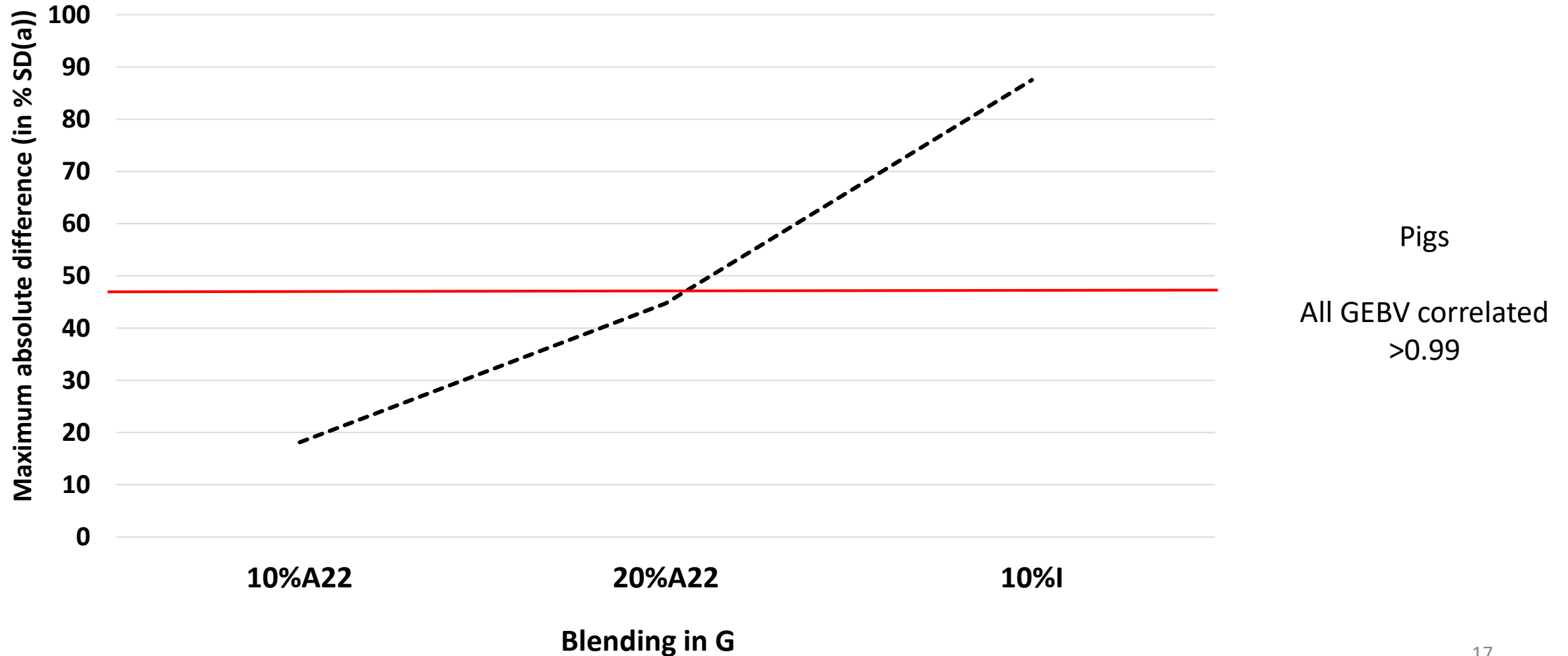
| Reliability | Average deviation in additive SD | | | |
|-------------|----------------------------------|----------|-------------|--------------|
| | All | 1 in 100 | 1 in 10,000 | 1 in million |
| 0.80 | 0.40 | 1.04 | 1.56 | 1.96 |

Average change for outliers

$$GEBV = rel * BV + rel(1 - rel)N(0, \sigma_a^2)$$

| Reliability | Average deviation in additive SD | | | |
|-------------|----------------------------------|----------|-------------|--------------|
| | All | 1 in 100 | 1 in 10,000 | 1 in million |
| 0.80 | 0.40 | 1.04 | 1.56 | 1.96 |
| 0.99 | 0.1 | 0.26 | 0.39 | 0.49 |

Changes in GEBV with different blending relative to 0.05 A₂₂



Conclusions

- More fluctuations in genomic evaluations than in BLUP
- Fluctuations of GEBV with APY due to choice of core animals
- Little impact on accuracy/reliability with sufficient number of core animals (EIG98 to EIG99)
- Fluctuations in line with reliabilities and normal distribution

Acknowledgements

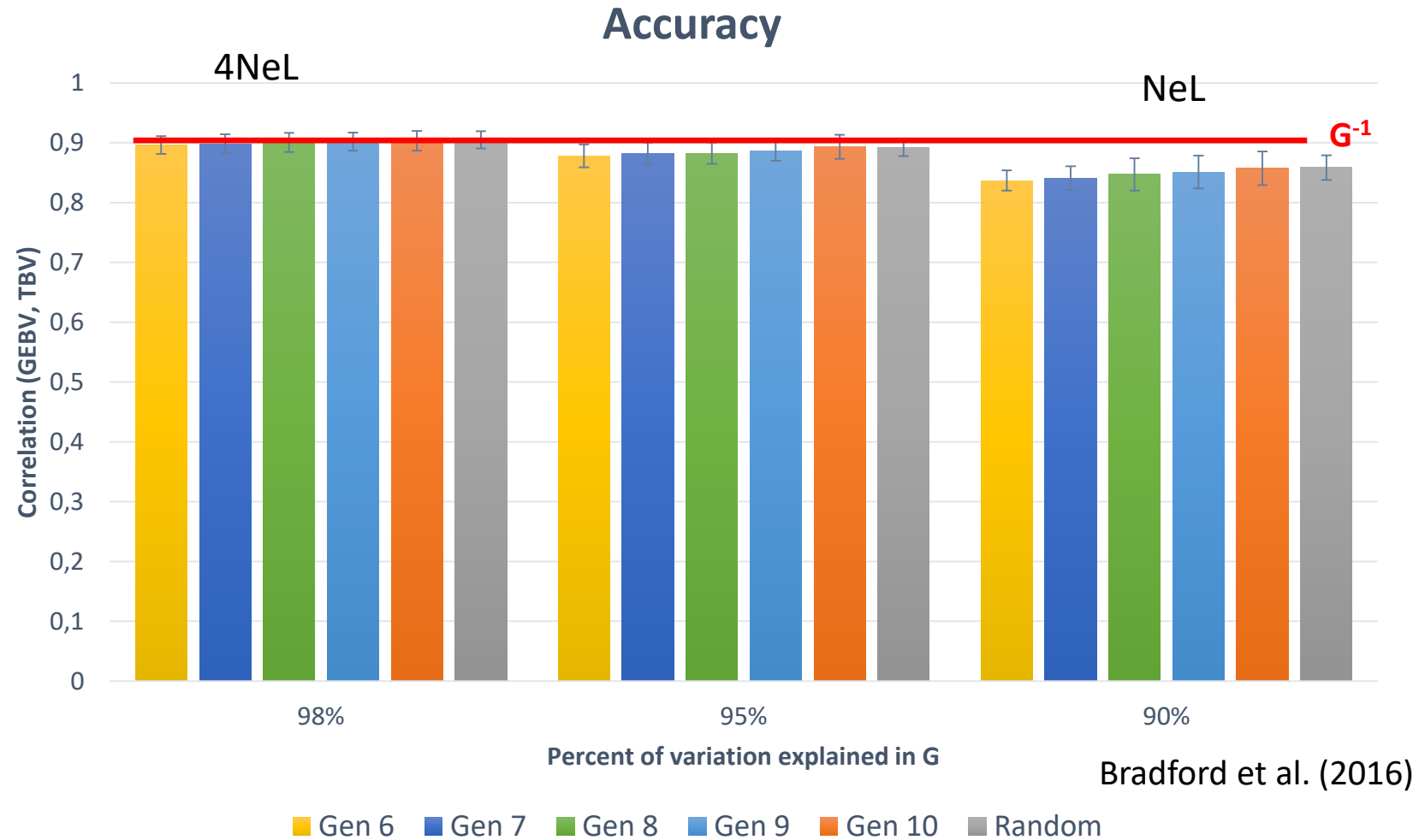
Tom Lawlor
Paul VanRaden



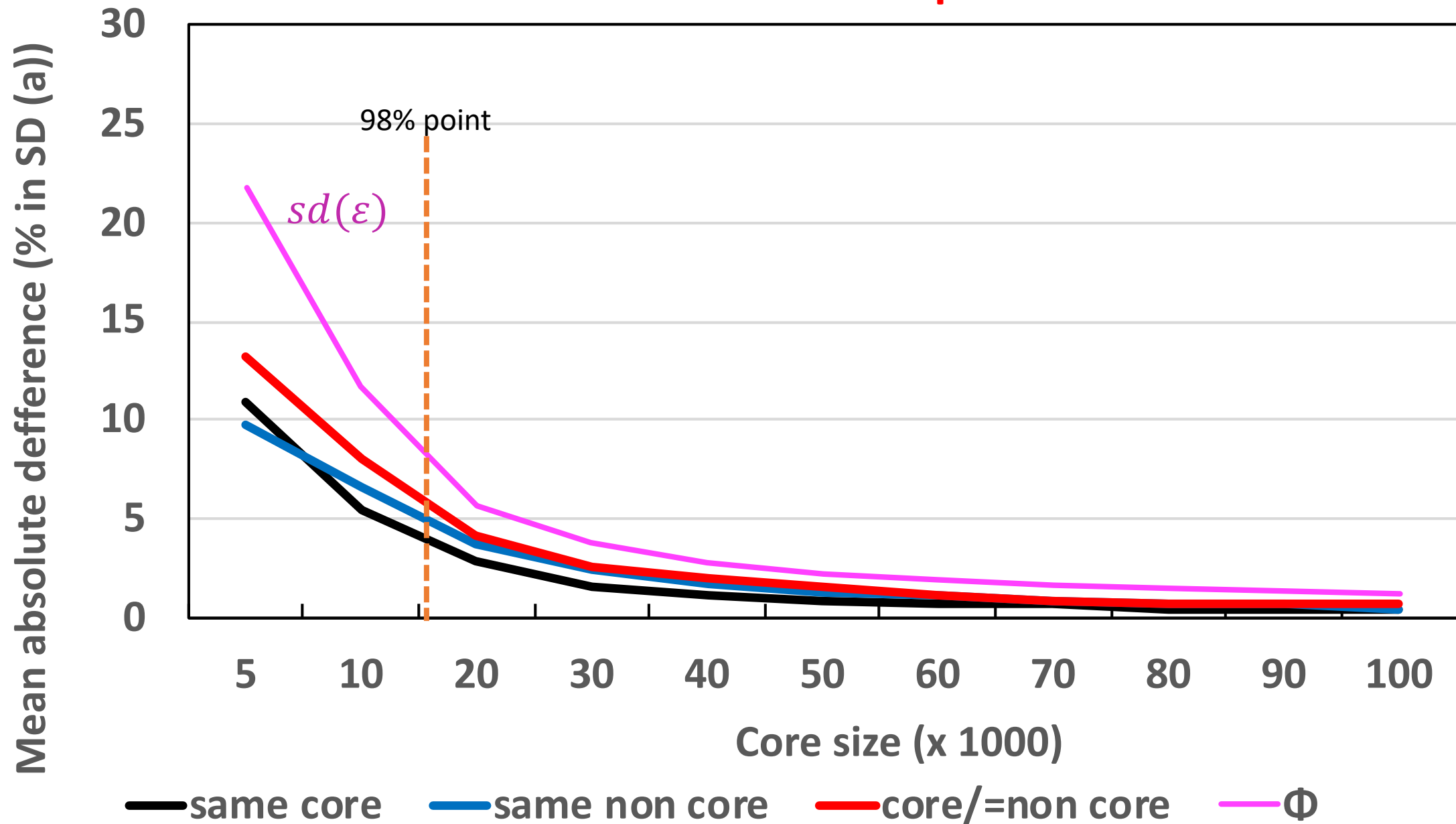
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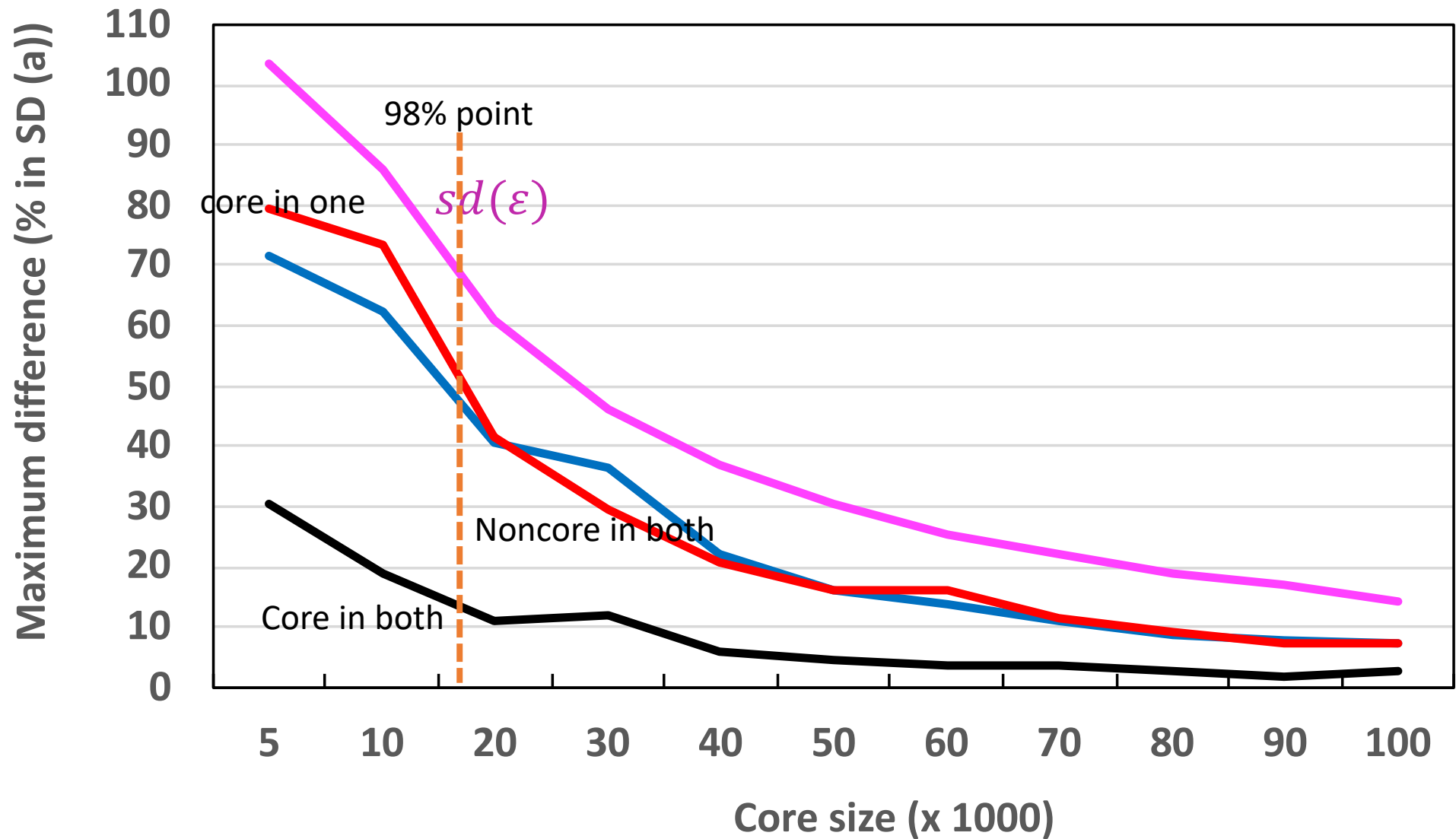
Which core animals in APY?



US Holsteins - udder depth



US Holsteins - udder depth



— same core — same non core — core/=non core — Φ