



THE UNIVERSITY
of EDINBURGH



Biotechnology and
Biological Sciences
Research Council



THE ROYAL
SOCIETY

Estimating haplotype and mutation effects in the context of genome sequence via ancestral recombination graphs

Gabriela Mafra Fortuna, Jana Obsteter, Ajda Moskric, Gregor Gorjanc



2024 EAAP, Florence

@GregorGorjanc @HighlanderLab

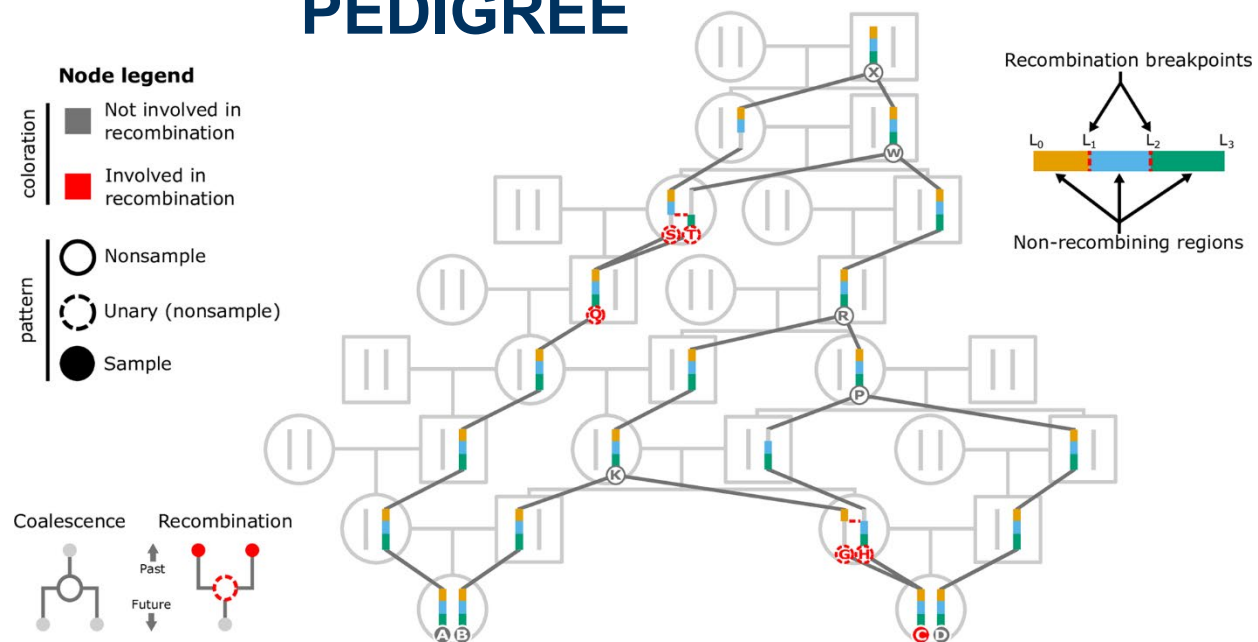


Ancestral Recombination Graph (ARG)

- **Representation of DNA variation by focusing on DNA events**
 - *branch/coallescent events* (where DNA molecule split/merge),
 - *mutation events* (where DNA molecule changes), and
 - *recombination events* (where DNA molecules exchange)
- **Insight into evolutionary history**
(time and place of DNA events, demography, divergence, introgression, ...)
- **Succinct data representation!**
(can handle large scale WGS datasets)

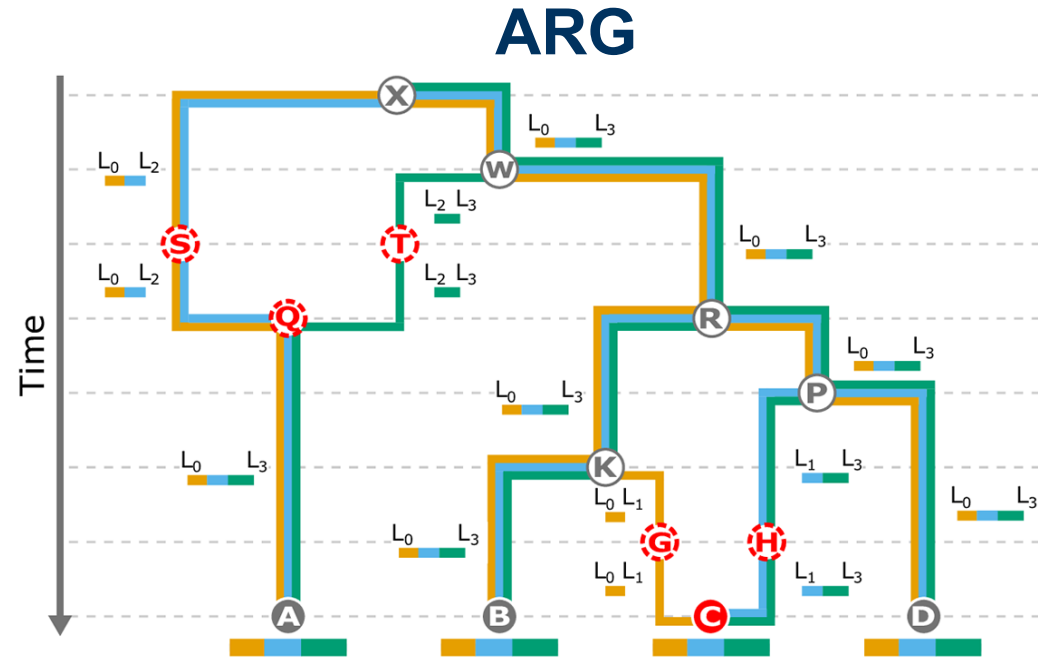
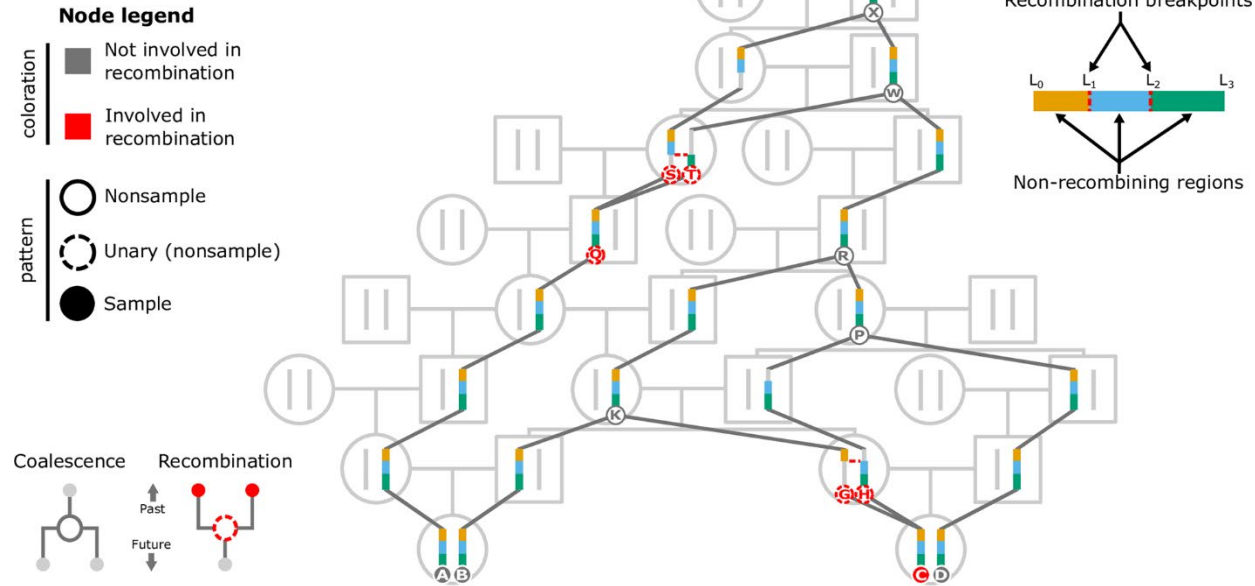
How do ARGs look like?

PEDIGREE



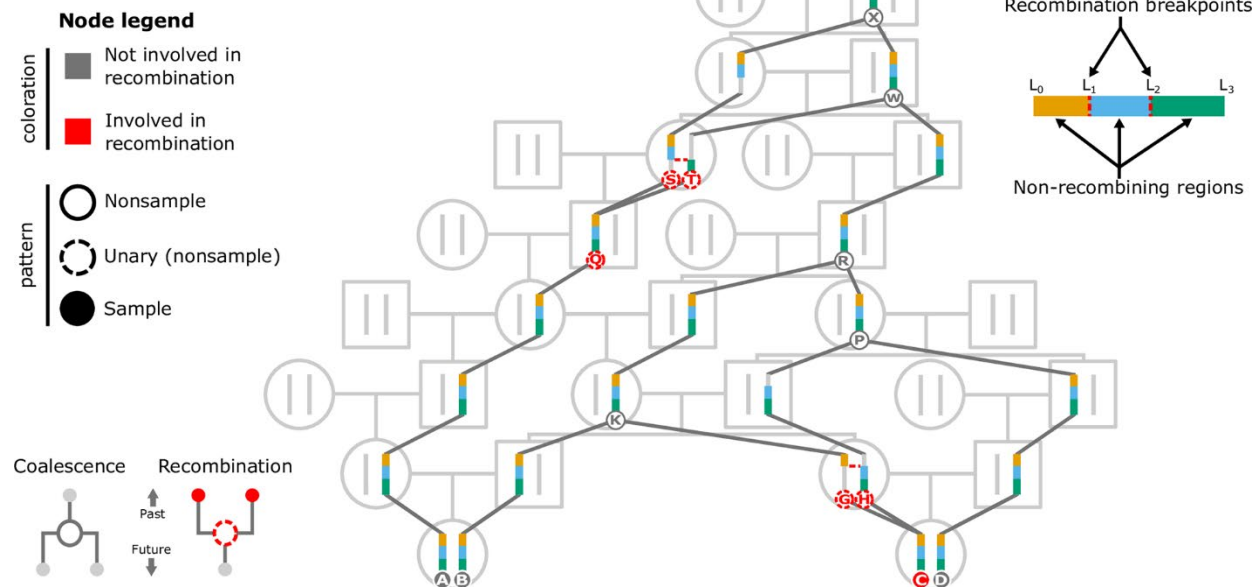
How do ARGs look like?

PEDIGREE

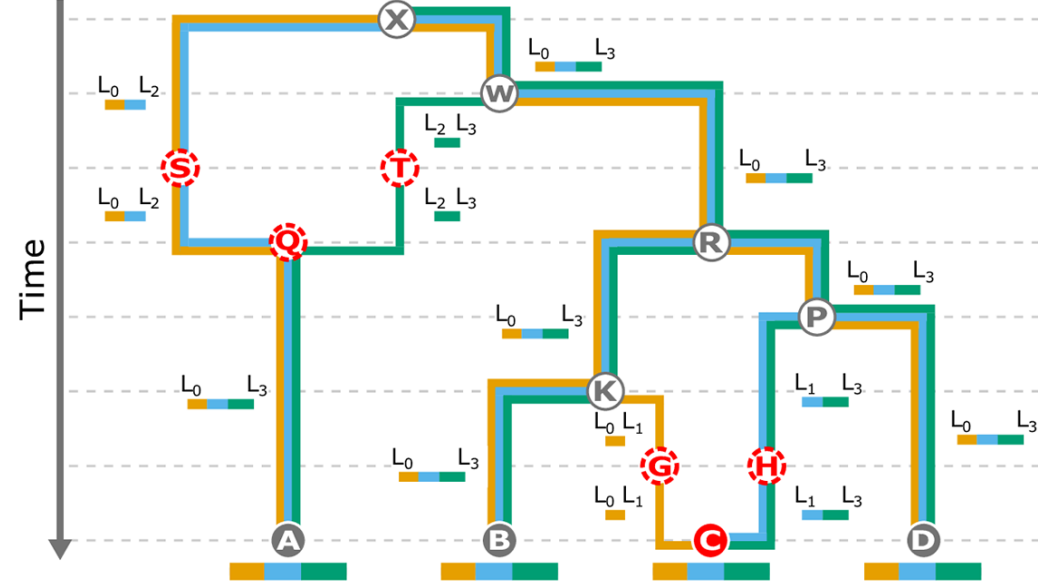


How do ARGs look like?

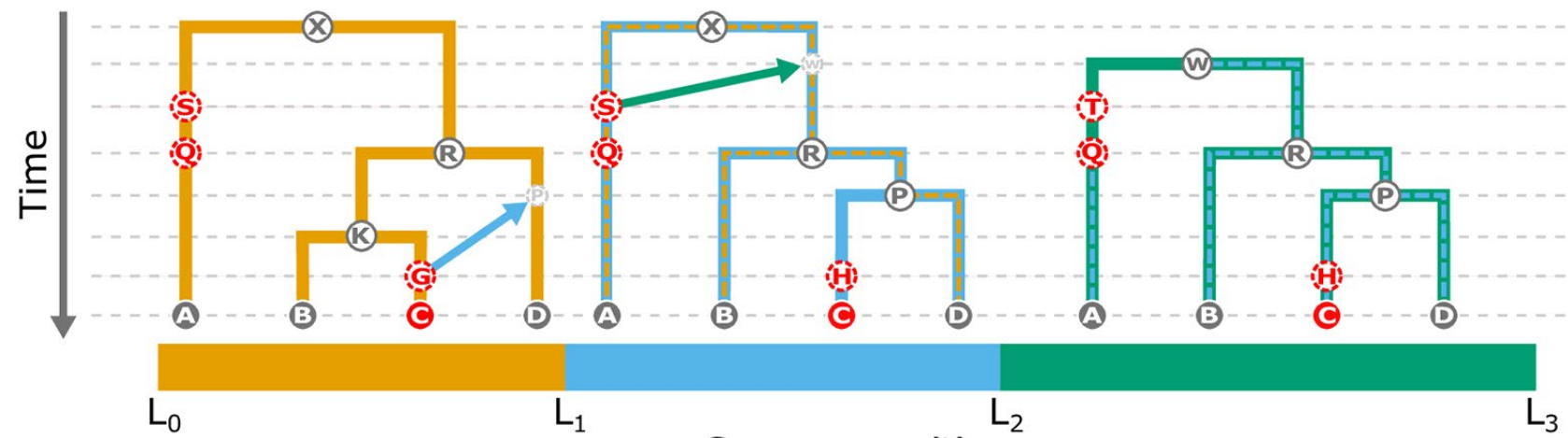
PEDIGREE



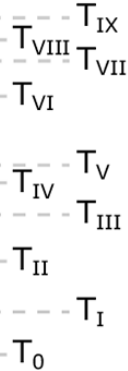
ARG



LOCAL TREES



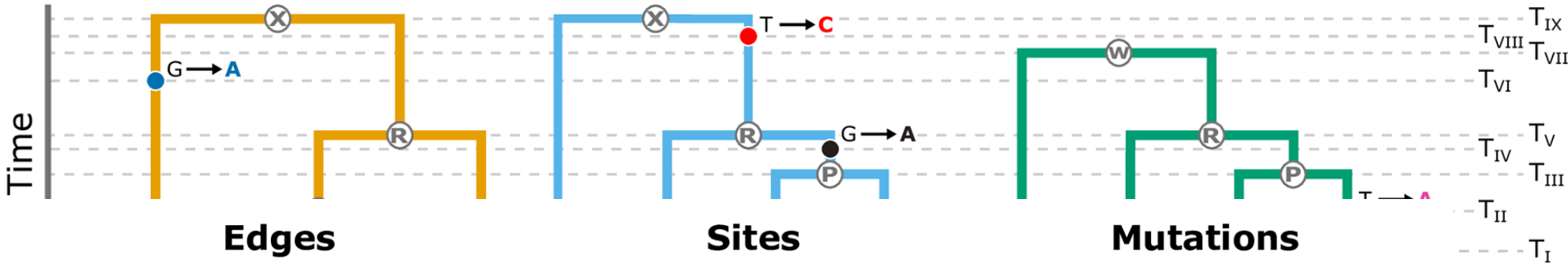
■ ■



Genotypes → Haplotypes → ARG

Sample

	Site ID											
	0	1	2	3	4	5	6	7	8	9	10	11
A	G	T	A	G	T	C	G	T	A	T	A	T
B	G	T	G	G	C	C	G	T	A	T	A	C
C	G	T	G	G	C	C	A	T	A	T	A	C
D	G	T	G	G	C	C	A	T	A	T	A	C



Nodes

Node ID	Age
A	T ₀
B	T ₀
C	T ₀
D	T ₀
K	T _{II}
P	T _{III}
R	T _V
W	T _{VII}
X	T _{IX}

Edges

Genome start	Genome end	Parent	Child
L ₀	L ₂	X	A
L ₀	L ₁	K	B
L ₀	L ₁	K	C
L ₀	L ₂	X	R
L ₀	L ₁	R	D
L ₀	L ₁	R	K
L ₁	L ₃	R	B
L ₁	L ₃	R	P
L ₁	L ₃	P	C
L ₁	L ₃	P	D
L ₂	L ₃	W	A
L ₂	L ₃	W	R

Sites

Site ID	Position	Ancestral
0	S ₀	G
1	S ₁	T
2	S ₂	G
3	S ₃	G
4	S ₄	T
5	S ₅	C
6	S ₆	G
7	S ₇	T
8	S ₈	A
9	S ₉	T
10	S ₁₀	A
11	S ₁₁	C

Mutations

Mutation ID	Site	Node	Derived	Age
0	2	A	A	T _{VI}
1	4	R	C	T _{VIII}
2	6	P	A	T _{IV}
3	9	D	A	T _{II}
4	11	A	T	T _I

L₃

Ancestral Recombination Graph (ARG)

- **Representation of DNA variation by focusing on DNA events**
 - *branch/coalescent events* (where DNA molecule split/merge),
 - *mutation events* (where DNA molecule changes), and
 - *recombination events* (where DNA molecules exchange)
- **Insight into evolutionary history**
(time and place of DNA events, demography, divergence, introgression, ...)
- **Succinct data representation!**
(can handle large scale WGS datasets)
- **AIM: Quantitative genetic modelling based on ARGs!?**

TODAY: QG model for non-recombining DNA

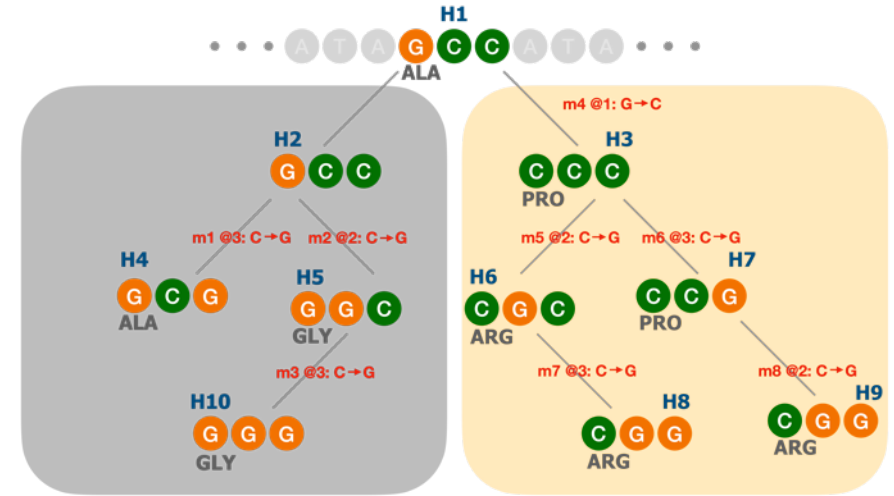
Model options:

- a) SNP-BLUP
- b) G-BLUP

Based on

- 1. Allele dosages

$$\begin{array}{c} \text{Allele} \\ \text{dosages} \end{array}
 \mathbf{X} =
 \begin{array}{c} \text{Individual} \end{array}
 \begin{array}{c} \text{SNP} \end{array}
 \begin{pmatrix}
 0 & 1 & 1 \\
 0 & 1 & 1 \\
 1 & 1 & 1 \\
 0 & 1 & 0 \\
 0 & 0 & 1 \\
 1 & 0 & 1 \\
 1 & 1 & 0 \\
 1 & 0 & 0 \\
 1 & 0 & 0 \\
 0 & 0 & 0
 \end{pmatrix}$$



TODAY: QG model for non-recombining DNA

Model options:

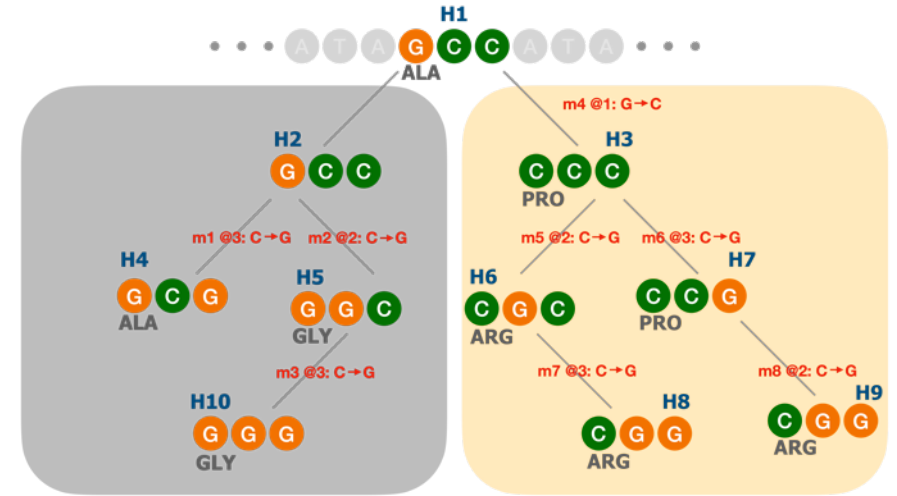
- a) SNP-BLUP
- b) G-BLUP

Based on

- 1. Allele dosages
- 2. Mutation dosages

$$\begin{array}{c} \text{Allele} \\ \text{dosages} \end{array}
 \quad
 \mathbf{X} =
 \begin{array}{c} \text{Individual} \\ \begin{pmatrix} 0 & 1 & 1 \\ 0 & 1 & 1 \\ 1 & 1 & 1 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \\ 1 & 0 & 1 \\ 1 & 1 & 0 \\ 1 & 0 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \end{array}
 \quad
 \begin{array}{c} \text{SNP} \end{array}$$

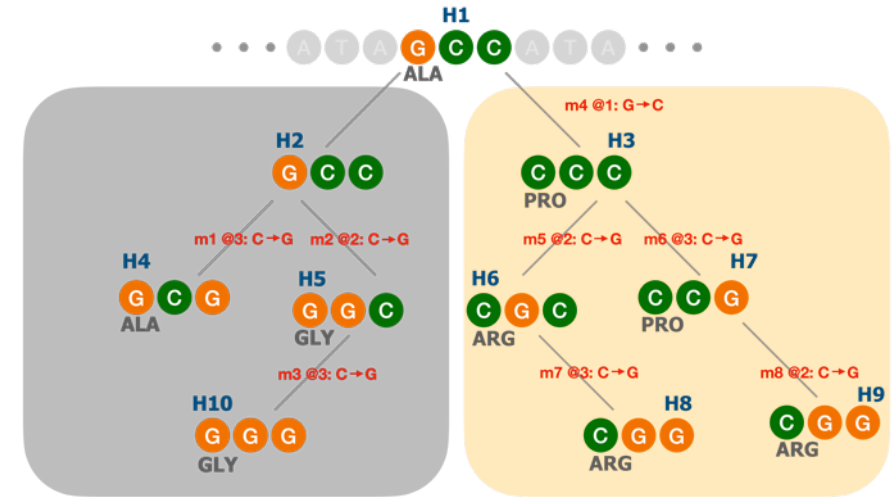
$$\begin{array}{c} \text{Mutation} \\ \text{dosages} \end{array}
 \quad
 \mathbf{X} =
 \begin{array}{c} \text{Individual} \\ \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 1 & 0 & 0 & 1 & 0 & 1 & 0 & 0 \\ 1 & 0 & 0 & 0 & 1 & 0 & 1 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 & 1 \end{pmatrix} \end{array}
 \quad
 \begin{array}{c} \text{Mutation} \end{array}$$



TODAY: QG model for non-recombining DNA

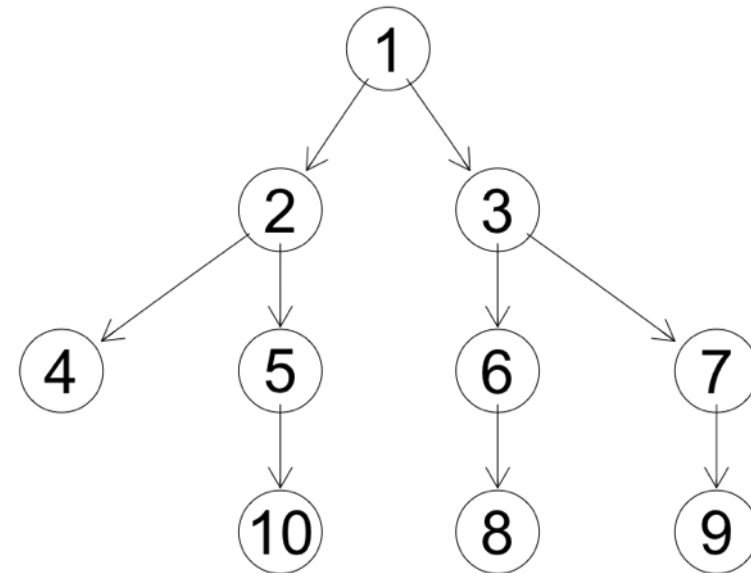
Model options:

- a) SNP-BLUP
- b) G-BLUP
- c) Tree-BLUP / ARG-BLUP



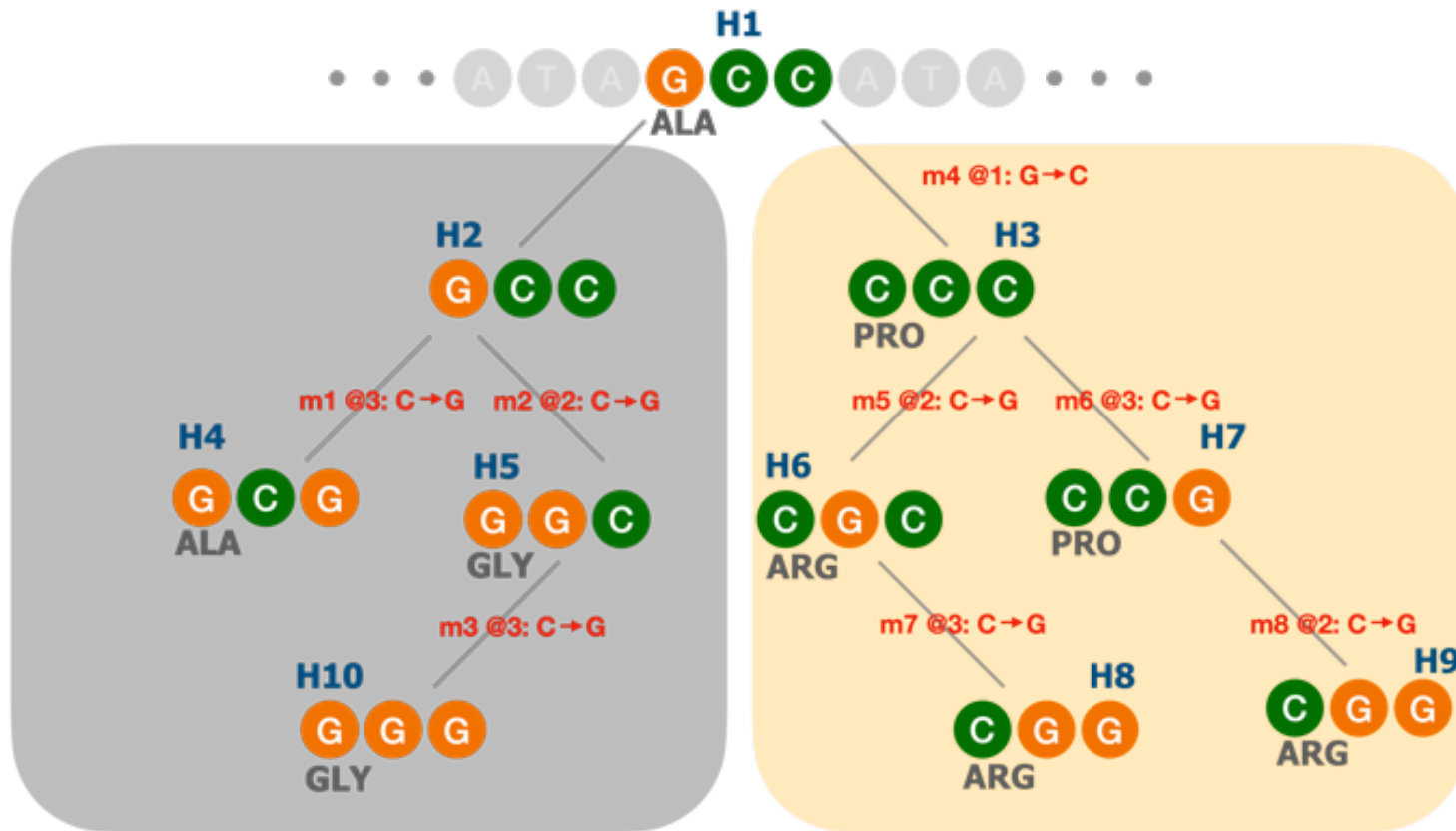
Based on

- 1. Allele dosages
- 2. Mutation dosages
- 3. Tree / ARG structure



Haplotype tree model

Haplotype's value can be modelled as the value of it's parental haplotype plus an “innovation” term
(mutation, structural variants, unobserved biology, epistasis, ...)



$$h_1 \sim N(0, \sigma_h^2)$$

$$h_2 \sim N(0, \sigma_h^2)$$

$$h_2 | h_1 \sim N(h_1, \sigma_m^2)$$

...

$$h_2 = h_1 + e_2$$

$$h_3 = h_1 + m_{1 \rightarrow 3} + e_3$$

$$h_4 = h_2 + (m_{2 \rightarrow 4} + e_4)$$

Tree-BLUP

- Phenotype model

$$\mathbf{y} = \mathbf{1}b + \mathbf{Z}\mathbf{h} + \mathbf{e}$$

- Haplotype tree model

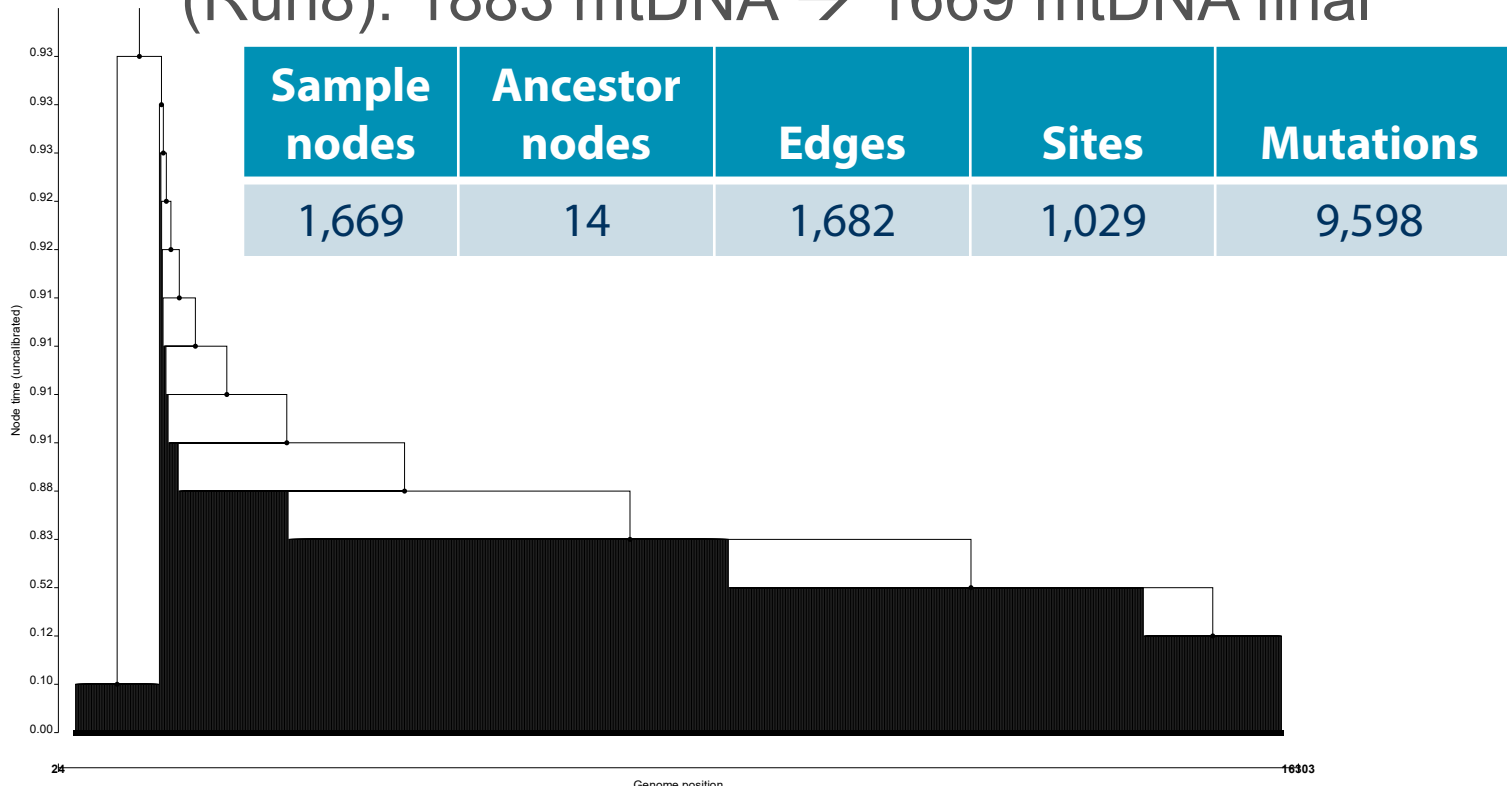
$$\mathbf{h} \sim N(\mathbf{0}, \mathbf{H}(\sigma_m^2 + \sigma_\epsilon^2))$$

- Covariance coef. matrix between haplotypes $\mathbf{H}$ has a simple inverse (precision matrix) due to DNA tree structure
- Can fit with most linear mixed model software (ASReml, blupf90, INLA, Mix99, MixBLUP, ...)

Proof of concept – real data + simulations

- **Real data**

- Cattle mtDNA
- Inferred mtDNA ancestral alleles
- Inferred mtDNA tree for 1000 Bull Genomes (Run8): 1883 mtDNA → 1669 mtDNA final



Simulations

ALL all mutations are causative

FEW 10% of mutations are causative

DIFF all mutation effects are different

SAME mutation type defines effect

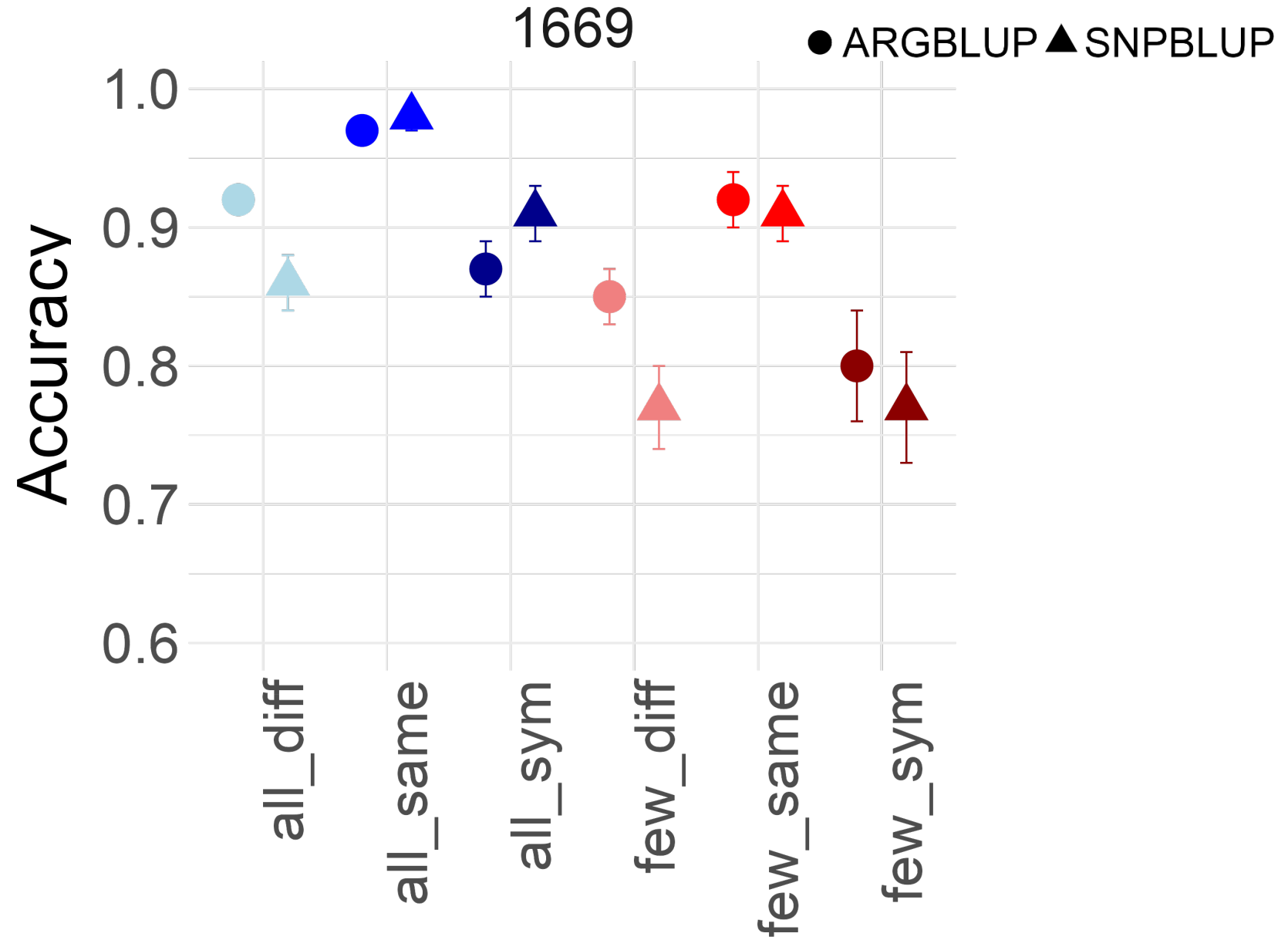
SYM symmetric mutation effects

1669 phenotypes

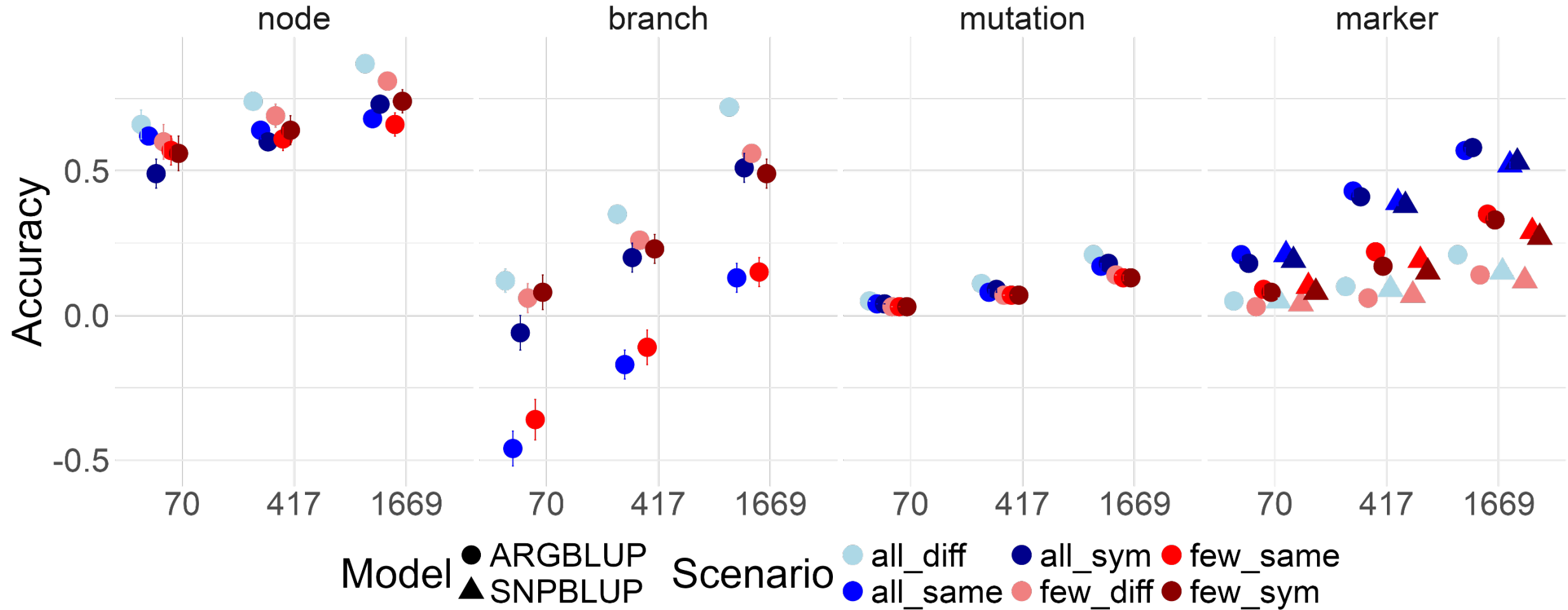
417 phenotypes

70 phenotypes

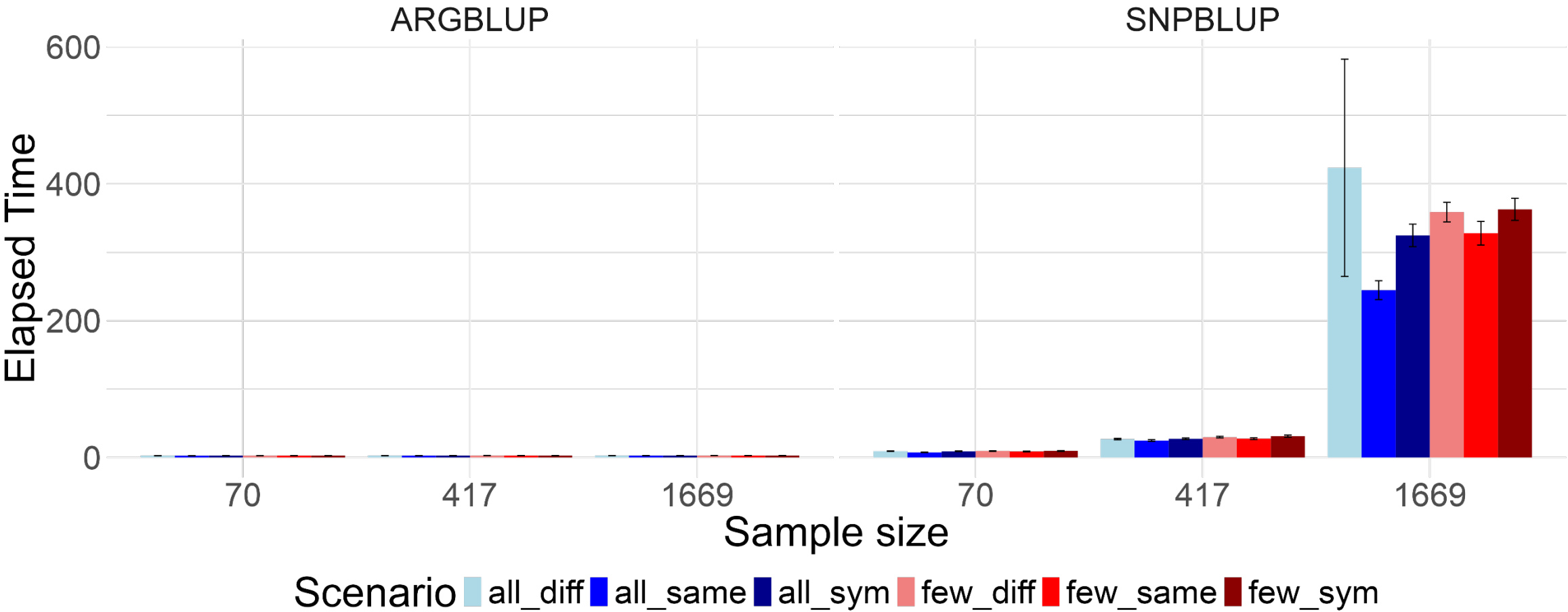
Accuracy of estimated haplotype effects (samples/tips)



Accuracy of various estimated effects



Execution time with INLA (seconds)



Conclusion

- Ancestral Recombination Graphs (ARGs) are the ultimate object in population genetics/genomics → now feasible & popular
- We are interested in quantitative genetic modelling with ARGs
- Here we presented a Tree-BLUP to work with a single non-recombining DNA region (mtDNA real data & simulation)
- QG modelling with the full ARG involves recombination events (haplotypes of different lengths) → we have a good working model for that in the pipeline



THE UNIVERSITY
of EDINBURGH



Biotechnology and
Biological Sciences
Research Council



THE ROYAL
SOCIETY

Estimating haplotype and mutation effects in the context of genome sequence via ancestral recombination graphs

Gabriela Mafra Fortuna, Jana Obsteter, Ajda Moskric, Gregor Gorjanc



2024 EAAP, Florence

@GregorGorjanc @HighlanderLab

